Evolution of Learning Rules for Supervised Tasks II: Hard Learning Problems

Ibrahim KUSCU
Cognitive and Computing Sciences
University of Sussex
Brighton BN1 9QH

Email: ibrahim@cogs.susx.ac.uk

November 10, 1995

${\bf Abstract}$

Recent experiments with a genetic based encoding schema are presented as a potentially powerful tool to discover learning rules by means of evolution. The representation used is similar to the one used in Genetic Programming

the input variable(s)". This means that there is a direct correlation between particular input values and particular output values.

However, sometimes the rule may not refer to particular values of variables. Rather it may refer to possible 'relationships' among input values. It has been shown by Clark and Thornton [2] that learning behaviors based on some training sets which take into account the relationship among values of the input variables can be extremely difficult (named as type-2 learning problems). In one of the studies [10] well-known learning algorithms such as ID3, back-propagation and classifier systems are tested on a type-2 problem and all showed poor results.

In a previous paper [6] an encoding schema has been presented and tested on several simple supervised tasks. Combined with genetic algorithms it can successfully produce evolution of learning rules. Rather than searching for a general learning algorithm (as in the work of Chalmers [1]), the aim is to see whether evolution would produce a specific learning rule for the problem in hand. Although the representation schema is very similar to the one used by of Koza [5] in Genetic Programming (GP) paradigm, introducing prior knowledge into the representation of initial solutions using problem specific functions is minimal, if any at all. The main motivation to exclude problem specific functions is to see whether evolution can produce (i.e. discover) a learning rule which can, in some ways, represent those functions. In this strategy potential learning rules are encoded as random mathematical expressions at variable lengths and only four functions is allowed: plus, minus, multiplication and protected division. The terminal units can be random numbers and random variables. The variables are to be instantiated to input values of training set in a typical supervised learning. By using LISP's "EVAL" statement, the expressions are evaluated to certain numbers. This value is then mapped to a value in the range of value of target outputs through a squashing function and is used to determine the success of a potential rule in correctly learning the supervised task.

In this paper several experiments where the model is applied to hard learning problems such as three Monk's problems and parity problems will be presented. In the sections that follow, I will first describe the Three Monk's problems. Next, I will introduce Genetic Programming (GP) in relation to the Monks problems. The following section contains the representation strategy and the process of applying genetic algorithms. Then the experiments and the results will be presented. Finally, I will conclude with a discussion and future research possibilities using the genetic based encoding schema.

2 Three MONK's Problems

The three MONK's problems are used to compare the performance of different symbolic and non-symbolic learning techniques [11] including AQ17-DCI, AQ17-FCLS, AQ14-NT, AQ15-GA, Assistant Professional, mFOIL, ID5R-hat, TDIDT, ID3, AQR, CN2, CLASSWEB, ECOBVEB, PRISM, Backpropagation

and Cascade Correlation.

MONKS's problems involve classification of robots which are described by six different attributes. The attributes and their possible values are as follows:

ATTRIBUTES	VALUES
head_shape	round, square, octagon
body_shape	round, square, octagon
${\tt is_smiling}$	yes, no
holding	sword, balloon, flag
${ t jacket_color}$	red, yellow, green. blue
${\tt has_tie}$	yes, no

Each of the three problem requires learning of a binary classification task. Whether the robot belongs to a particular class or not is decided based on the following rules:

```
Problem M1: (headshape=bodyshape) or (jacketcolor= red)

Problem M2: Exactly two of the six attributes have their first value.

Problem M3: (jacketcolor = green and holding = sword) or (jacketcolor = (not blue) and bodyshape = (not octagon))
```

The most difficult one among these problems is the second problem since it refers to a complex combination of different attribute values and is very similar to parity problems. Problem one can be described by standard disjunctive normal form (DNF) and may easily be learned by all symbolic learning algorithms such as AQ and Decision Trees. Finally, problem three is in DNF form but aims to evaluate the algorithms under the presence of noise. The training set for this problem contains 5 percent misclassification.

The results of the comparison have shown that only Backpropagation, Backpropagation with decay, cascade correlation and AQ17-DCI had 100 percent p11.7602Td.880112Td(propagatr940(noise.)]TJn]TJ77.280Monkroblem)-1180(all(proon)1000ad9s)Tj10.31

2.0.1 Training and Testing Sets

The training and testing sets used for the experiment in this paper are the same as those used by Thrun in the performance comparison experiments. In these experiments two different sets are used. The first set adapted an original coding for the problems where each of the attributes would have one of the following values:

```
attribute#1 : {1, 2, 3}
attribute#2 : {1, 2, 3}
attribute#3 : {1, 2}
attribute#4 : {1, 2, 3}
attribute#5 : {1, 2, 3, 4}
attribute#6 : {1, 2}
```

Thus the rules describing the true cases can be reformulated as below:

```
MONK-1:
(attribute_1=attribute_2) or (attribute_5=1)

MONK-2:
(attribute_n = 1)
for EXACTLY TWO choices of n (n {1,2,...,6})

MONK-3:
(attribute_5 = 3 and attribute_4 = 1) or
(attribute_5 != 4 and attribute_2 != 3)
```

The second set of training and testing cases for the problems are the conversion of the original coding into the binary coding. Obviously, this has a direct effect on the rules describing the true cases and the formulation of the problems. The number of input variables increases from 6 to 17 since each possible value of the attributes is represented as 3 digit binary numbers where each digit represents the presence of a specific value of the attributes.

2.1 Genetic Programming

In the genetic Programming Paradigm of Koza [5] problems of Artificial Intelligence (AI) are viewed as the discovery of computer programs which produce desired outputs for particular inputs. The computer programs can be an expression, formula, plan, control strategy, decision tree or a model depending on the sort of AI problem.

He claims that solving AI problems requires searching the space of all possible computer programs for the fittest individual computer program. Genetic Programming (GP) is the method of searching for this fittest individual computer program based on Darwinian natural selection and genetic operations.

Genetic programming steps, as in the application of conventional Genetic Algorithms (GA), involve initialisation of random population of computer programs and for a number of generation, evaluating the fitness of the individual programs and applying genetic operators.

One of the important feature of the GP is that it uses variable length of genome (i.e. computer programs) which reflects hierarchical and dynamical aspects of the potential solutions to a particular problem. Since the shape and the size of the solution to a problem may not be known in advance, specification or restriction of the potential solutions to certain format may limit the search space so that it may be impossible to reach a solution. By moving from fixed length genotype to the adaptation of variable length genotype, GP improves the capabilities of conventional GA.

In GP the genotype (i.e. computer programs) is composed of a set of functions and terminal units appropriate to the problem domain. The set of terminals are either some variable atoms or some constants. The set of functions would include arithmetic operations, mathematical functions, programming operations, boolean operations or any other domain specific functions.

typical GP practice would favor using XOR function since it would drastically facilitate finding a solution and the solution would be simple and elegant. Experiments in this paper aim to discover such specialised functions by starting the search with more general functions which can define the specialised functions.

In GP practice a typical function set for each of the Monks' problems would probably, at least, be as shown below in F function sets for each of the problem:

For all of the three problems, I will use only protected division, multiplication, plus, minus and a squashing function which maps the value of an expression after it is EVALuted to a value in the range of 1 to 0 (see later discussion).

F* =

The expression: (*I1* - ((*I2* + 1) * 0))

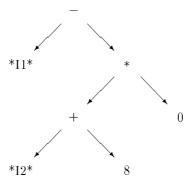


Figure 1: Tree representation of an expression.

5. If the solution found or sufficient number of generations are created then stop; if not go to 2.

The initialization technique is randomly generating mathematical expressions. This introduces the least amount of domain specific knowledge into the initial population through the variables used in the expressions. Unlike Koza's genetic programming applied to particular problems there are no domain specific functions. Only four mathematical functions are allowed; addition, subtraction and multiplication and protected division.

3.2.1 Evaluation

In order to provide a basis to determine the fitness of the expressions, each generation the expressions are evaluated using Lisp's "EVAL" statement by instantiating input values for each of the patterns from the training set.

The fitness of an expression is based on its success in learning a specific task. Since the target outputs are in the range of 0 to 1, the values, once obtained

showed the most success, especially in mapping to binary target outputs, was the following:

```
if value > 1 return 1
if value < 0 return 0
otherwise return the value</pre>
```

The fitness (success) of the individual expression is computed by testing them on all training patterns, and dividing the total error by the number of patterns, subtracting from 1 and multiplying by 100 yielding a fitness percentage between 0 and 100.

The expressions are ranked after each generation according to their success. Those who are higher in the rank (higher scoring ones) are said to be most fitting expressions.

3.2.2 Selection

The purpose of selection in GA is to give better opportunity of reproducing to those members of the population which shows better fitness. For the model this means to select those expressions with higher scores (beginning part of the rank) and give them more chance to reproduce.

In the model, parent selection technique for reproduction is normalizing by using an exponential function taken from Whitley's [12] rank-based selection technique. The function generates integer numbers from 1 to population size. The generation of numbers exhibits characteristics of a non-linear function where there is more tendency to produce smaller numbers (since higher scoring expressions are on top of the rank).

The function is $Z = X - \sqrt{\frac{X*X - 4*(X-1)*Y}{2*(X-1)}}$ The selection algorithm is based on the X, Y, Z values in the above formula where X is a bias computed as 1+Y where Y is a random number between 0 and 1. The value of Z lies between 0 and 1 and in the rank-ordered population N the expression at position N*Z is chosen.

The number produced by this function is used as an index to the ranked population of expressions from highest scoring ones to the lowest scoring. Then, after producing two indices by using the selection function the corresponding expressions are selected to undergo the genetic operators.

3.2.3 Genetic Operators

Applying genetic operators introduces variation to the population of expressions and allows the components (genes) of better performing expressions to live longer. This creates the necessary environment to cause evolution. In order to accomplish this it uses two different genetic operators; crossover and mutation. However, implementation of the both of the operators used by the system

are different than conventional implementations on bit strings since the length of expressions is variable.

In order

MONK1 is not tested for binary coding). The parameters of GA include a

The results emphas1I

contains a relationship among the input variables. Although it is very difficult to get a successful performance on such problems, in general, the poor performance observed here is not solely due to the strategy employed in the experiments. This is proved to be the case as a result of our control experiment on the parity problems discussed later in the section. As it will be explained later in the discussion section, it has a close link with the way GP like practices.

(- (- (* *I12* *I13*) (+ *I6* *I14*))))

Evolved Learning Rules for MONK 3 (Original Coding)

The learning rule evolved for MONK 3 (original) is the simple but perfect solution discovered in terms of the functions and random numbers used. Here the range of random numbers was 10. The rule is easily understandable and corresponds exactly to the second part of 'OR' in the original learning rule of MONK 3: attribute five is not equal to four and attribute 2 is not equal to 3. Note that the evolved expression implicitly code for relative more specialised functions EQUAL, NOT and AND than arithmetical operators. This clearly demonstrates the power of the model as a potentially useful tool in discovering learning rules for learning problems. The resulting rules can sometimes be a complex and totally new representation or simple re-representations.

```
0.983607 0.935651
(- (* (- *I5* 4) (- *I2* 3)))))
```

4.1 Parity Problems: a control experiment

In order to test whether the poor result obtained on MONK2 is directly attributable to the coding strategy I have carried out a control experiment. It

The MONK2 and Parity problems are similar in that the learning rule describing either refers to some kind of relationship among the input variables. The general rule for parity problems states that the output is true if there are even number of true values among the input values. As it can be observed from the following results the model can code for the solutions to the supervised tasks where the learning rule describes a relationship among the input variables. However, when the problem gets larger and more complex (5 bit-parity or higher) it becomes more difficult for the model to code for the solution. In this case, a larger population size and an increase number of generations as well as longer and more complex representations of the solutions may be required. For example Koza in his experiments with even-5-parity problems increased the number of population from 4000 to 8000 to find a solution [5]p.533. This is a huge number compared to our 300 population size and 250 generations.

followings are the results of evolving learning rules for the parity problems. Note that for each of the problem our fixed set of functions are capable of coding at least for OR, AND and NOT.

Evolved Learning Rules for 2-Bit-Parity Problem

```
1.00
(|%| (- (- *I1* *I2*)) (- (- (+ *I1* (- (* *I2* *I2*))) *I2*)))
1.00
(+ (+ *I2* *I1*) (- (* *I2* (+ (- (+ *I1* *I1*)
(- (* *I2* (+ (- *I1* *I2*) *I2*)))) *I1*))))
```

Evolved Learning Rules for 3-Bit-Parity Problem

```
1.0
(+ (- (- (- (|%| *I1* (- (* (- (* *I2* *I1*)
(+ *I2* (* *I3* *I1*))) (+
(* (- (+ *I2* *I1*)) *I3*) *I1*))))) (+ (+ (- (* *I1* *I1*)) (*
(- (+ *I2* *I3*)) (- (+ *I1* (+ (- (- *I2* (- (* *I2* *I2*))))
*I1*)))) *I2*)) (- (- *I1* *I3*) *I1*)) (- (* (- (* (- (+ *I3*
*I3*) *I3*) (+ (- (|%| *I3* *I2*)) *I1*))) (- (- (- (- *I2* (-
(|%| (+ *I2* *I2*) *I2*)))))

1.0
(- (+ (- (- (|%| (- (* *I3* *I2*)) (* *I1* (- (|%| (- (+ *I2*
(+ *I1* (* *I1* (|%| *I3* *I3*))))) *I3*)))))
(+ *I2* (- (+ *I1* *I3*)))
(- (* (|%| *I1* (- (+ *I3* *I2*))) (- (- *I2* *I1*) *I1*)))) (|%|
(- (- (- (+ (- (- *I2* *I3*)) (- (- (- *I3* *I3*)) *I2*)) (- (- (+ *I1*
(* (+ *I1* *I2*) *I2*))) (- (* *I3* *I3*)))))
```

Evolved Learning Rules for 4-Bit-Parity

```
0.9375
(+ (+ (- (- (+ (+ *I2* (- *I4* (+ (- (* *I3* *I1*)) *I1*)))
(- (- (- (+ (|%| (* *I4* *I1*) *I2*) (- (|%| *I3*
(+ *I2* *I1*))))) (- (* (- (|%| *I4* *I3*)) (- *I2* *I3*))))))
(|%| (- (|%| *I4* (* *I1* (|%| *I1* (+ *I3* *I4*)))))
(* *I3* (+ *I1* *I2*)))) (- (|%| (- (- (* *I3* *I2*) *I3*))
(- (+ (- (|%| *I1* *I3*) *I4*) *I4*) (- (- *I4*
(- (+ (- (- (- (- *I4* *I3*)) *I2*) *I4*) *I2*))))))+
```

rule is described in terms of relationships among input values. This provides an additional support in favor of the second hypothesis. Moreover, when the problem gets larger and more complex (i.e. moving from 3 to 4 bit and higher parity problems), evolution of successful learning rules becomes more difficult. As the complexity and size of the problem increase, the current strategy of encoding should search for the larger space to find the solution. One of the problem comes from the non-convergent characteristic of GP like methods. When a solution or a more fit individual is found during the course of the evolution, it can easily turn to be an unfit individual after the application of crossover. Although, as a

tion about the ability of GP like practices to generalize over the test cases. Although, recent experiments shows that the model can generalise over simple, linearly separable problems, there is no clear evidence whether it can successfully generalise over hard learning probelms. This issue should be one of the major concern for the next experiments.

References

- [1] D.J. Chalmers. Evolution of learning: an experiment in genetic connectionism. In Touretzky et al, editor, *Connectionist Models*. Morgan Kaufmann, 1990.
- [2] A. Clark and C. Thornton. Trading spaces: Computation, representation and the limits of learning. Technical Report 291, COGS, University of Sussex, 1993.
- [3] D. Goldberg. Genetic Algorithms in Search, Optimization and Machine Learning. Addison-Wesley, Massacheusettes, 1989.
- [4] J. Holland. Adaptation in Natural and Artificial Systems. University of Michigan Press, Ann Arbor, USA, 1975.
- [5] J. Koza. Genetic Programming:On the programming of computers by means of natural selection. MIT press, 1992.
- [6] Ibrahim Kuscu. Evolution of learning rules for supervised tasks i: Simple learning problems. Technical Report CSRP-394, Uni. of Sussex, COGS, 1995.
- [7] Ibrahim Kuscu. Incrementally learning the rules for supervised tasks: Monk's problems. Technical Report CSRP-396, Uni. of Sussex, COGS, 1995.
- [8] Una-May O'Reilly and Franz Oppacher. An experimental perspective on genetic programming. In R. Manner and B. Manderick, editors, Proc of 2nd Intl Conf on Parallel Problem Solving from Nature, pages 331-340, 1992.
- [9] D. Rumelhart, G. Hinton, and R. Williams. Learning internal representations by error propagation. In D. Rumelhart, J. McClelland, and the PDP Research Group, editors, Parallel Distributed Processing: Explorations in the Micro-structures of Cognition. Vols I and II. MIT Press, Cambridge, Mass., 1986a.
- [10] C. Thornton. Supervised learning of conditional approach: a case study. Technical Report 291, COGS, University of Sussex, 1993.

- [11] S. Bala et al Thrun. The monk's problems a performance comparison of different learning algorithms. Technical Report CMU-CS-91-197, School of Computer Science, Carnegie-Mellon University., USA, 1991.
- [12] D. Whitley. The genitor algorithm and why rank based-based allocation of reproductive trials is best. In J.D. Schaffer, editor, *Proceedings of Third iInternational Conference on Genetic Algorithms*, pages 116–123, 1989.